

**RUHR-UNIVERSITÄT BOCHUM**  
**IMPLEMENTING THE AUGMENTED EPSILON-CONSTRAINT METHOD FOR MULTI-OBJECTIVE OPTIMISATION OF ENERGY SYSTEMS**

# Agenda

- Introduction
- Implementation
- Case Study
- Conclusion & Outlook

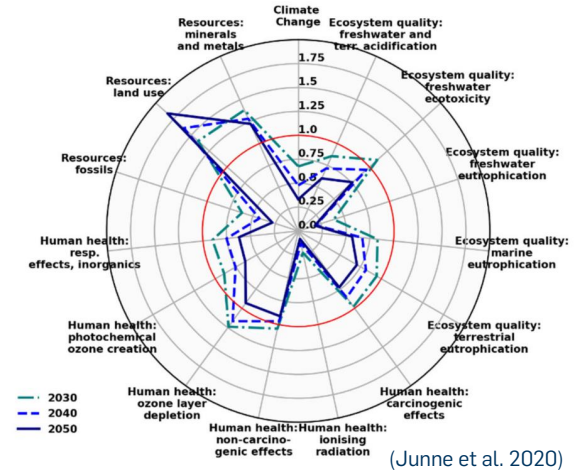
# Introduction

# Why Energy System Modelling?

- Energy sector transformation to mitigate climate change
- Structural changes
  - Intermittent renewables increase flexibility requirements (temporal, spatial and sectoral)
  - Increased number of stakeholders
- Energy system models provide insights and support complex decisions

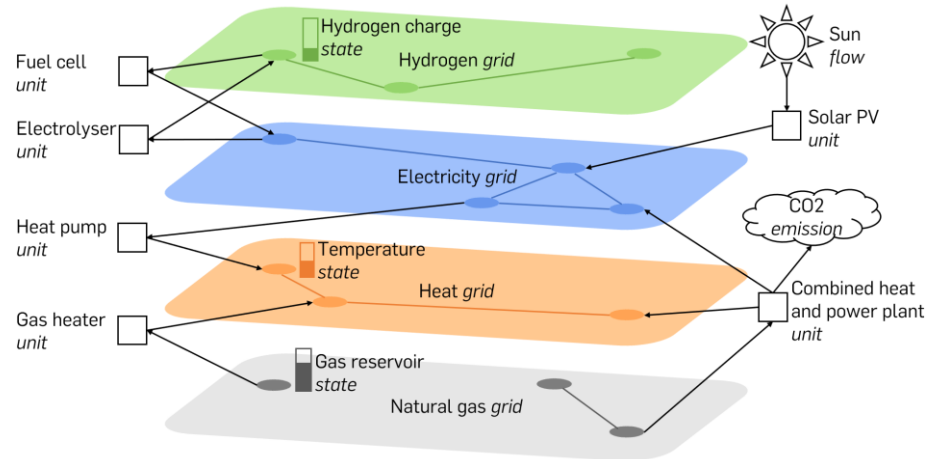
## Why Multiple Objectives?

- Conflicting interests have to be balanced
- Environmental sustainability is multi-criteria concept in itself
- Feasible and “interest-optimal” scenarios to support decisions



# Energy System Optimisation Framework Backbone

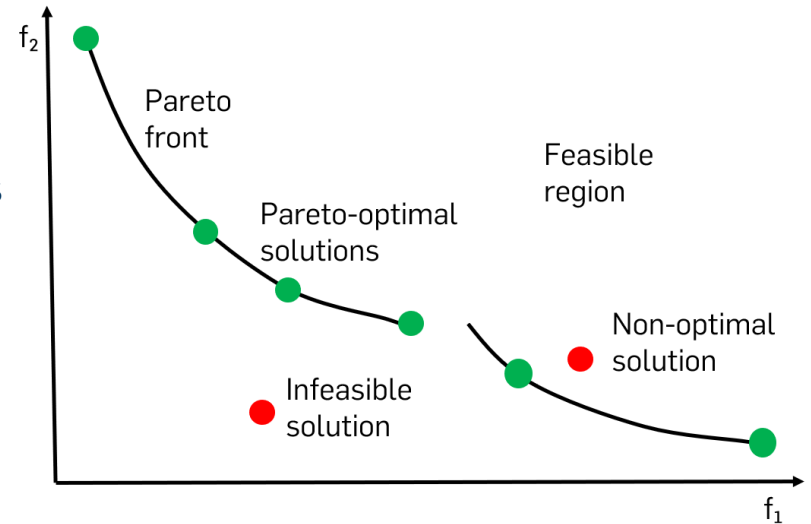
- Network Model
  - Highly adaptable structure
  - Various energy carriers and sectors
  - Flexible spatial and temporal resolution
  - High technological detail
  - Stochastic modelling
- Optimisation
  - Investment and operational planning
  - Cost minimisation
  - Various constraints
- Open Source



$$\begin{aligned}
 v_{BB}^{obj} = & \sum_{f,t} p_{f,t}^{probability} \cdot \left( v_{f,t}^{vomCost} + v_{f,t}^{fuelCost} + v_{f,t}^{startupCost} + v_{f,t}^{shutdownCost} + v_{f,t}^{rampCost} + v_{f,t}^{stateCost} + v_{f,t}^{penalties} \right) \\
 & + v_{fomCost} + v_{unitInvestCost} + v_{lineInvestCost}
 \end{aligned}$$

# Multi-Objective Optimisation – General Principles

- Consider simultaneous optimisation of multiple real objective functions
- Notion of optimum: set of Pareto-optimal solutions, the so called *Pareto-front*
- A solution is called *Pareto-optimal* if improvements of one objective necessarily lead to deterioration of another
- Preferences are key to making decisions between optimal alternatives
  - express preferences before (*a priori*) or after optimisation (*a posteriori*)
  - express preferences and optimise iteratively (interactive)



# Augmented Epsilon-Constraint Method (AUGMECON)

- Advantages
  - Each solution is Pareto-optimal
  - Suited for a posteriori and interactive methods
  - No convexity or continuity required
- Method
  - Reformulate all but one objective to constraints
  - Introduce slack variable for each constraint

$$\min_{x \in V} \{f_1(x), f_2(x), \dots, f_k(x)\} \longrightarrow \min_{x \in V} \left( f_j(x) + c \sum_{i \in K} s_i \right) \quad \text{s.t.} \quad f_i(x) + s_i = \varepsilon_i \quad \forall i \in K \setminus \{j\}$$

- Further developments improve performance for 4+ objectives and integer variables, e.g. AUGMECON 2 and AUGMECON-R

Mavrotas, *Effective implementation of the epsilon-constraint method in Multi-Objective Mathematical Programming problems*, Applied Mathematics and Computation 2009.

Mavrotas and Florios, *An improved version of the augmented  $\varepsilon$ -constraint method (AUGMECON2) for finding the exact pareto set in multi-objective integer programming problems*, Applied Mathematics and Computation 2013.

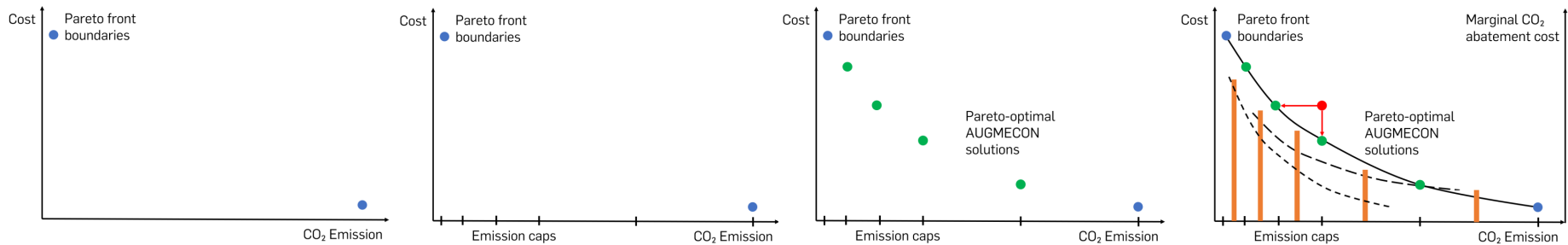
Niklas et al., *A robust augmented  $\varepsilon$ -constraint method (AUGMECON-R) for finding exact solutions of multi-objective linear programming problems*, Operational Research 2020.

Implementation



# General Remarks

- Implementing AUGMECON with Backbone for the two objectives cost and CO2 emission
- Two parts: new features in Backbone and “external” python code with 4 steps to run different versions of Backbone
- Illustrative purpose, method **adaptable** to more and other objectives
- Method is easily parallelisable, therefore **scalable**
  - Large and complex systems
  - Many objectives



# Step 1 – Determine Pareto front boundaries

- “External”: Lexicographic optimisation

$$\min_{x \in V} \text{cost}(x) \text{ s.t. } \text{emission}(x) = \min_{x \in V} \text{emission}(x)$$

$$\min_{x \in V} \text{emission}(x) \text{ s.t. } \text{cost}(x) = \min_{x \in V} \text{cost}(x)$$

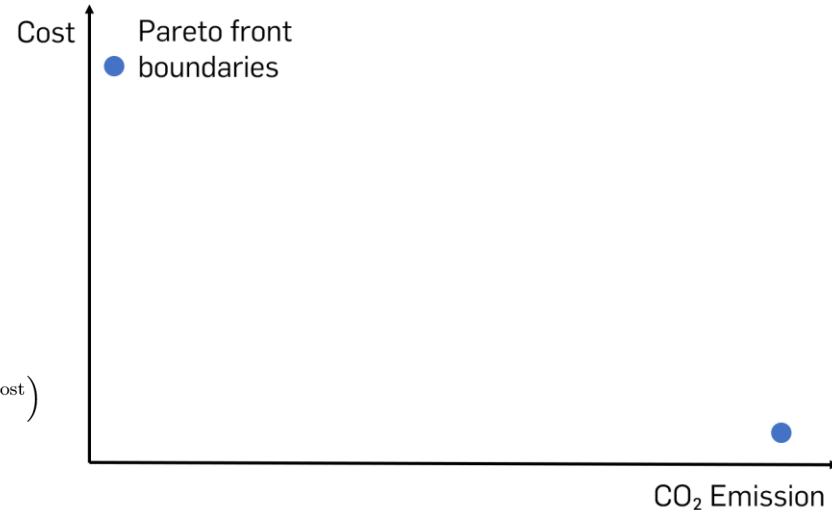
- New feature in Backbone

- Emission minimisation...

$$v_{\text{CO}_2}^{\text{obj}} = \sum_{f,t} p_{f,t}^{\text{probability}} \cdot \left( v_{f,t,\text{CO}_2}^{\text{generationEmission}} + v_{f,t,\text{CO}_2}^{\text{startupEmission}} + v_{f,t}^{\text{penalties}} \right)$$

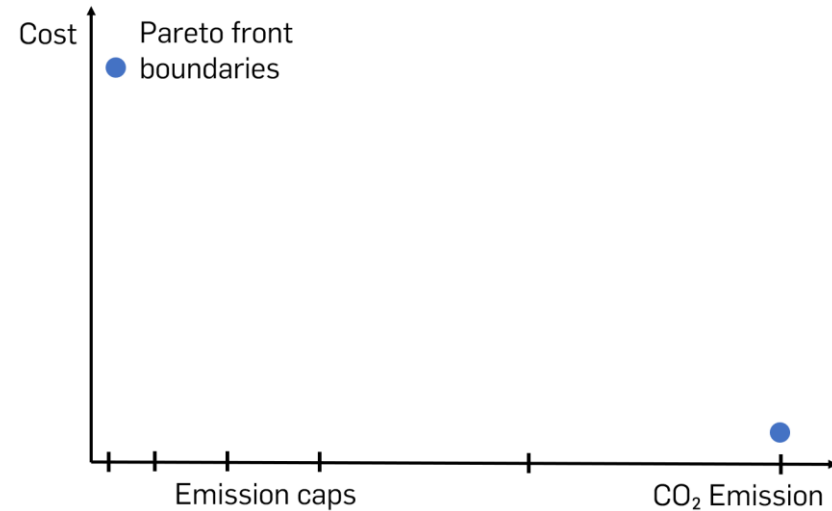
- ...with constrained cost

$$\sum_{f,t} p_{f,t}^{\text{probability}} \cdot \left( v_{f,t}^{\text{vomCost}} + v_{f,t}^{\text{fuelCost}} + v_{f,t}^{\text{startupCost}} + v_{f,t}^{\text{shutdownCost}} + v_{f,t}^{\text{rampCost}} + v_{f,t}^{\text{stateCost}} \right) + v^{\text{fomCost}} + v^{\text{unitInvestCost}} + v^{\text{lineInvestCost}} \leq p^{\text{costLimit}}$$



## Step 2 – Decide on emission caps

- Decide on emission caps within boundaries from Step 1, then all are feasible
- Number and distribution of solutions can well be controlled for sufficiently regular models, as desired by the modeller



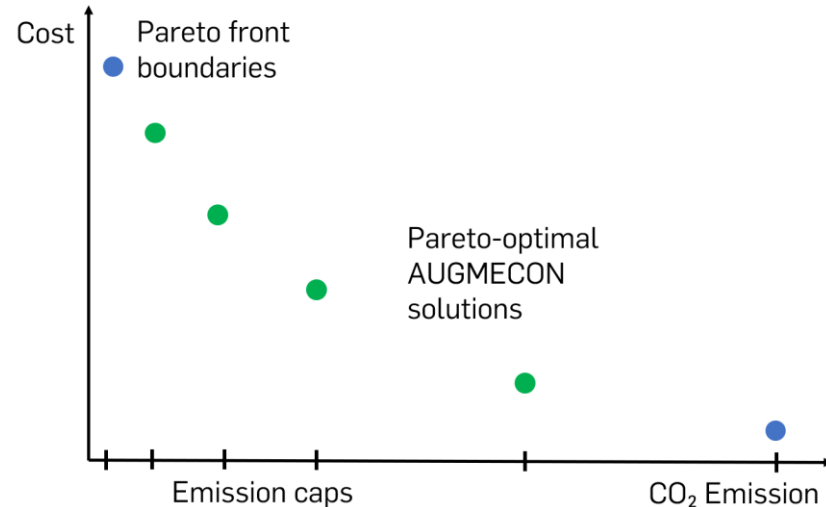
# Step 3 – Calculate Pareto-optimal Solutions

- “External”: Run AUGMECON implementation once for each emission cap from Step 2
- New feature in Backbone
  - Add slack variable to cost objective...

$$v_{\text{AUGMECON}}^{\text{obj}} = v_{\text{BB}}^{\text{obj}} + c \cdot s$$

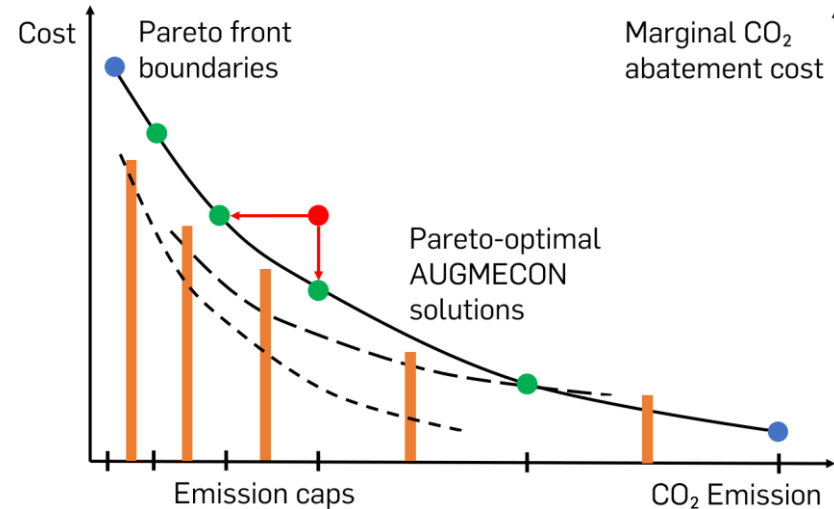
- ... and reformulate emission constraint

$$\sum_{f,t} p_{f,t}^{\text{probability}} \cdot \left( v_{f,t,\text{CO}_2}^{\text{generationEmission}} + v_{f,t,\text{CO}_2}^{\text{startupEmission}} \right) = p_{\text{CO}_2}^{\text{emissionCap}} + s$$



# Step 4 – Conduct Further Analyses

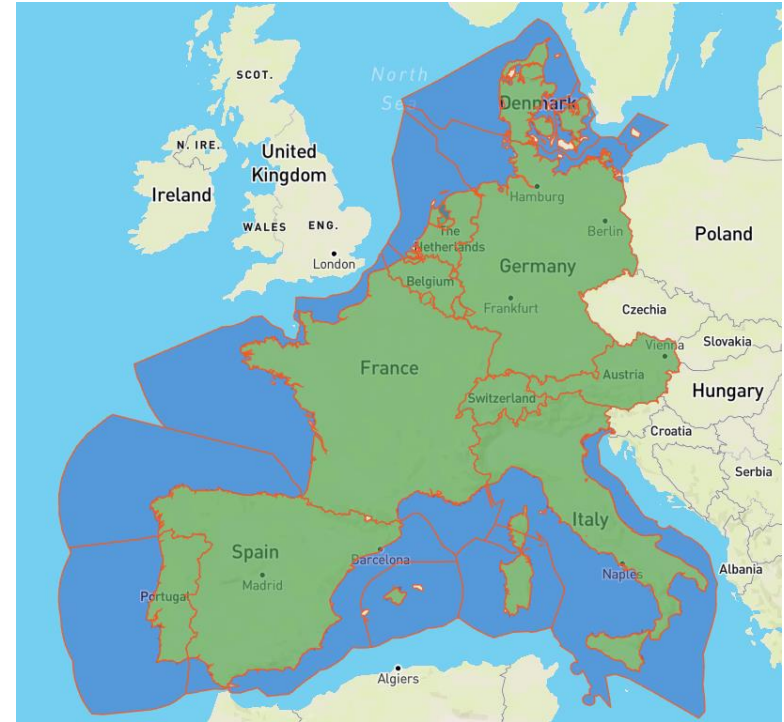
- Analyse emission reduction scenarios “as usual”
- Approximate Pareto front from discrete solutions (solid black line)
- Vary assumptions to get different Pareto fronts (dashed black lines)
- Quantify trade-off between objectives, e.g. marginal CO<sub>2</sub> abatement costs (orange bars)
- Compare exogenous scenario to Pareto front and analyse potential improvements (red dot and arrows)



# Case Study

# Western & Southern European Power System Model

- Power network model based on PyPSA-Eur
- Including 11 countries
- Modelling one year at hourly resolution
- Investment planning for
  - Generation: solar PV, onshore & offshore wind, gas
  - Storage: battery, hydrogen
- Cost and demand assumptions for 2050<sup>1</sup>
- Main limitations
  - Electricity sector only
  - Geographical boundaries

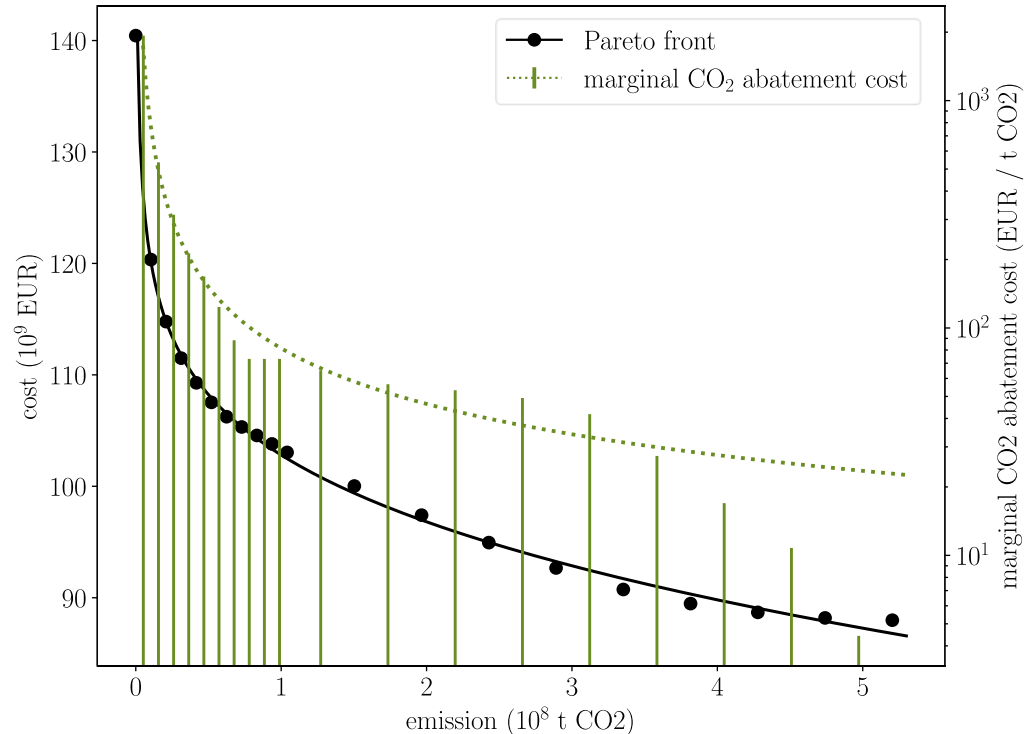


Hörsch et al., *PyPSA-Eur: An Open Optimisation Model of the European Transmission System*, Energy Strategy Reviews 2018. (See also <https://github.com/PyPSA/pypsa-eur>)

<sup>1</sup> Largely based on Pietzcker et al., *Tightening EU ETS targets in line with the European Green Deal: Impacts on the decarbonisation of the EU power sector*, Applied Energy 2021.

# Results – Pareto Front and Trade-Offs

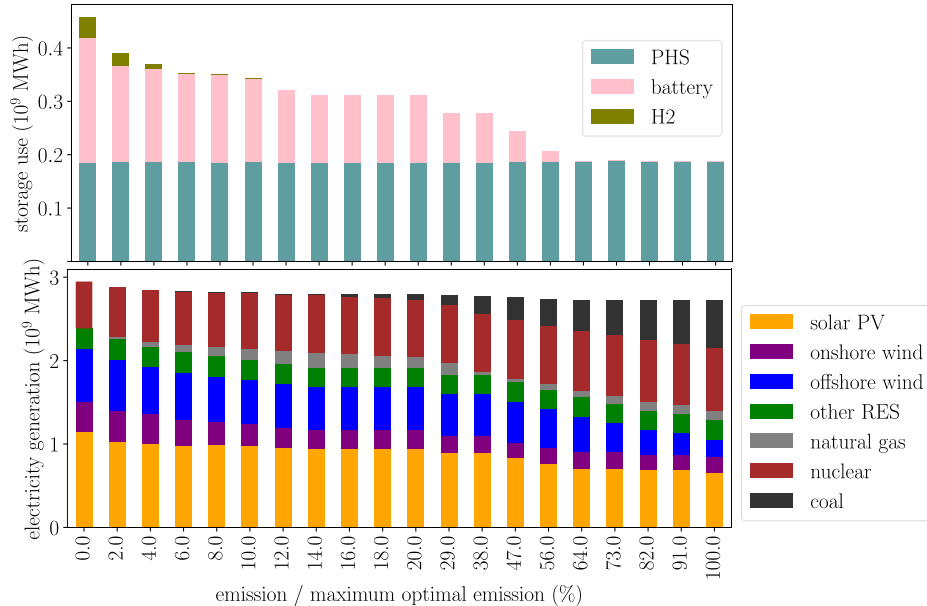
- Objectives' ranges
  - 90...140  $\times 10^9$  €
  - 0...5.2  $\times 10^8$  t CO<sub>2</sub>
- Marginal CO<sub>2</sub> abatement cost
  - 5...2000 € / t CO<sub>2</sub>
- CO<sub>2</sub> reductions of up to 90% at marginal abatement costs below 100 € / t CO<sub>2</sub>



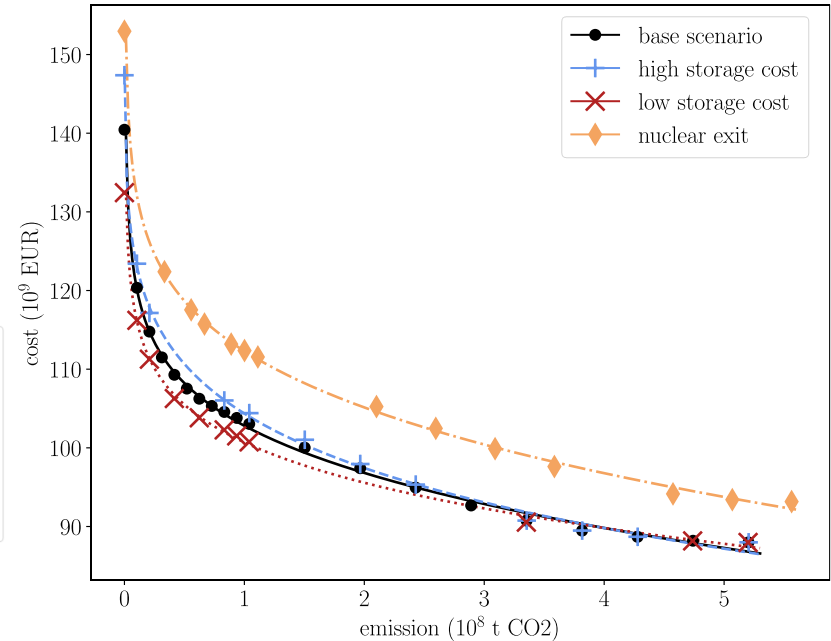


# Results – Further Analyses

- Generation and storage mix across different CO<sub>2</sub> reduction scenarios



- Nuclear exit (BE, DE, ES) and sensitivity of storage cost (battery  $\pm$  25%, H<sub>2</sub>  $\pm$  15%)



# Conclusion & Outlook

# Conclusion & Outlook

- The implementation enables for energy systems to
  - determine **cost-emission-optimal solutions** and their **objective range** and
  - further analyse and compare scenarios, e.g. regarding **trade-offs** or **assumptions**.
- The implementation is **adaptable** and **scalable** to various energy systems and objectives.

## Future work

- Combine life cycle assessment and energy system modelling – see Sophie Pathe´s work<sup>1</sup>
- Include more objectives and improve algorithm for that
- Ease exploration of 4+D Pareto front to support decision making

<sup>1</sup> Pathe, S. & Bertsch, V. (2021) Electricity system expansion planning of the Rheinish mining area considering environmental impacts by using multi-criteria-optimization. Work in progress.

Thank you for your attention!